

## Control Design for Shunt Active Power Filter Based on p-q Theory in Photovoltaic Grid-Connected System

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### ABSTRACT

This paper presents the control for Shunt Active Power (SAPF) filter in photovoltaic (PV) systems connected to the grid. The proposed configuration of the system consists of a photovoltaic array that connected to the grid through the three-phase inverter topology that also serves as an active filter. Photovoltaic is coupled in parallel with the direct current (DC) side of the active filter. With this configuration, can be obtained three advantages, namely the elimination of harmonic currents caused by nonlinear load, reactive power injection, and injection of active power generated photovoltaic. The p-q Theory is used to calculate the harmonic reference current to be used to control the active filter coupled photovoltaic in generating anti-harmonic currents. The results show that system can reduce harmonic distortion from THD 27.22% to be THD 1.05%, whereas when the active power from photovoltaic injected, the THD become 2.01%. Power sharing can also be seen from this study.

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## 1. INTRODUCTION

The development of power electronics equipment that used as an interface between the load and the electrical system affects the power quality in particular the emergence of electrical harmonics [1]. the power electronics converter is a nonlinear load that injects the harmonic current on the grid. the non linear load is the main cause of harmonic distortion that occurs in the electrical system. Variable Speed Drives (VSD), Uninterruptible Power Supply (UPS), Switched Mode Power Supply (SMPS) [2].

Harmonic distortion causes some unexpected conditions on the electrical system. Harmonic distortion can decrease the accuracy of the electrical meter. Harmonic distortion may also cause excessive dissipation of electrical equipment so as to increase the cost of the bill. Furthermore, harmonic distortion causes electrical equipment not to work on the specified power quality standards causing a decrease in the lifetime of the electrical equipment [3].

Passive filter is one method used to reduce current harmonic distortion. These passive filters use a combination of inductors and capacitors to eliminate harmonics at a predetermined frequency. The drawback of this is a passive filter harmonic compensation provided is fixed, so it can not eliminate the frequency harmonics that are not specified [4]. Active Power Filter (APF) has advantages that can eliminate various frequency harmonics that arise. In active power filter, there are an inverter and controllers to control the compensation current to eliminate the harmonic currents distortion that arise [5]-[6]. Shunt active power filter (SAPF) arranged in parallel with the non-linear load. The shunt active power filter has advantages in dimension than in series type [7].

The p-q Theory introduced by Professor Akagi in 1983 [8]. This Theory explains the concept of active and reactive power in the instantaneous calculation algorithm. Then, the p-q Theory developed in the application of power flow calculations and harmonic distorted component calculations to determine the reference current [9]-[11].

The generation of reference current of active power filter influenced by the performance of active power filter control system in response to the load changes. Closed-loop control proportional-integral (PI) is used to regulate DC side voltage and power flow of active power filter [12]-[14]. The use of closed-loop control systems improve the accuracy of p-q Theory in the generation of the reference current in the range of larger currents.

Research and development of photovoltaic grid-connected systems has increased very significantly in the last two centuries. Three-phase inverter Sinusoidal Pulse width modulation (SPWM) control system used to transfer active power that generated by photovoltaic into the grid [15]-[18].

This paper, photovoltaic coupled in parallel with the shunt active power filter so that with this system, the shunt active power filter not only can reduce harmonic currents but also can supply the active power that generated by photovoltaic. P-q theory is used to control active power filters in determining harmonic reference currents.

The contribution of this paper is to combine the functions of an active power filter into the photovoltaic grid-connected systems so that by the proposed design system, it will be obtained three advantages, namely harmonic current compensation, reactive power compensation, and the of active power compensation that generated by photovoltaic. Basic p-q Theory is modified to perform the function of active power compensation. Photovoltaic array voltage is increased by using quadratic boost converter with a voltage conversion ratio is relatively larger than conventional boost converter.

**2. SYSTEM DESIGN**

**2.1. Shunt Active Power Filter In Photovoltaic Grid-Connected System**

The active power filter design on Photovoltaic Grid-Connected System consists of two main components, namely the shunt active power filter which are arranged in parallel with a nonlinear load, and photovoltaic that arranged in parallel with the DC side voltage of the Voltage Source Inverter (VSI). Active power filter serves to eliminate harmonics at the source based on the control system that used. In addition, the active filter also serves to compensate for reactive power into the load [19]. Active power filter coupled photovoltaic can inject active power to be supplied into the grid. Notation SAPF+PV show shunt active filter system coupled photovoltaic.

Figure 1 shows the configuration of the filter active in photovoltaic grid-connected system. Active power filters coupled photovoltaic connected to the distribution network through a Point of Common Coupling (PCC) through the LF inductor. The LF Inductor is not as inductor for passive filter but as an inductor coupling that serves as a filter switching VSI [20].

The DC voltage at the photovoltaic array is connected to the DC-DC to obtain high DC voltage [21]-[22]. Quadratic converter is used as a DC-DC converter because the ratio of input and output voltages are relatively large [23]. The layout of inductors, capacitors, diodes, and switch on quadratic boost converter as shown in Figure 2. Correlation of the input and output voltage of quadratic boost converter as in the following Equation (1):

$$\frac{V_{out}}{V_{in}} = \frac{1}{(1-D)^2} \tag{1}$$

where D is the duty cycle.

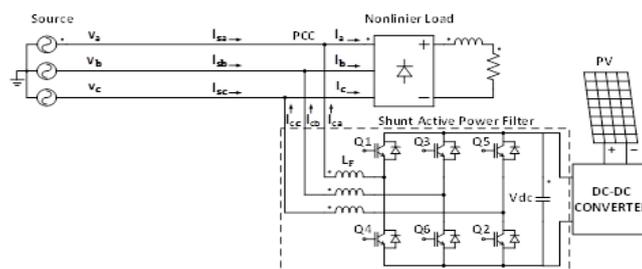


Figure 1. Effects of selecting different switching under dynamic condition

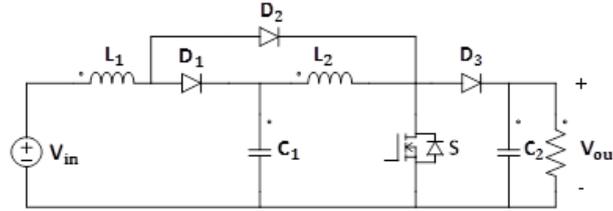


Figure 2. Quadratic converter topology

**2.2. Control System On The Shunt Active Power Filter Coupled Photovoltaic**

The p-q Theory is used to calculate the reference current of shunt active power filter. Reference current is a signal current waveform of the anti-harmonics current. Then, the Reference current is used to control the switching pattern of shunt active power filter so that anti-harmonic current can be generated. Anti-harmonic current waveform is used to eliminate the harmonic current waveform.

The first step in the calculation of the reference current generation is to transform the three-phase voltages and currents in abc coordinates into two phases in αβ coordinates using clarke transformation. This transformation is necessary to simplify the calculation of instantaneous power at a later stage [24]. Equation (2) shows the Clarke transformation of voltage while equation (3) shows the current clarke transformation.

$$\begin{bmatrix} v_\alpha \\ v_\beta \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} v_a \\ v_b \\ v_c \end{bmatrix} \tag{2}$$

$$\begin{bmatrix} I_\alpha \\ I_\beta \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & -\frac{1}{2} & -\frac{1}{2} \\ 0 & \frac{\sqrt{3}}{2} & \frac{\sqrt{3}}{2} \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} \tag{3}$$

Based on the p-q Theory, instantaneous active and reactive power can be expressed in a multiplication operation voltages and currents in the αβ coordinates as in Equation (4).

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} v_\alpha & v_\beta \\ -v_\beta & v_\alpha \end{bmatrix} \begin{bmatrix} I_\alpha \\ I_\beta \end{bmatrix} \tag{4}$$

Instantaneous power p and q in equation (4) consists of the AC component (p~ and q~) and the DC component (P and Q). DC components are fundamental components while the AC component is a harmonic component, so that:

$$\begin{bmatrix} p \\ q \end{bmatrix} = \begin{bmatrix} P + p\sim \\ Q + q\sim \end{bmatrix} \tag{5}$$

To calculate the current value of the equation (4), the equation is reversed, so that would be obtained:

$$\begin{bmatrix} I_\alpha \\ I_\beta \end{bmatrix} = \frac{1}{v_\alpha^2 + v_\beta^2} \begin{bmatrix} v_\alpha & -v_\beta \\ v_\beta & v_\alpha \end{bmatrix} \begin{bmatrix} p \\ q \end{bmatrix} \tag{6}$$

Figure 3 shows the calculation step of p-q Theory in generating a reference current signal. The voltage and current on the source side is read by the sensor is then used as input for the calculation of the reference current generation. The reference current is then compared with the current compensation of active power filter using hysteresis current control method to produce a switching pattern on the VSI of active power filter.

From Equation (5) and Equation (6) can be seen that for eliminating reactive power from the source is to making negative value of q in equation (6). To separate the harmonic component to the fundamental component, p power only use the AC components. Then the P<sub>PV</sub> power of the photovoltaic added. Power losses in the VSI is represented as P<sub>loss</sub>. so that the reference current is:

$$\begin{bmatrix} I_{ca}^* \\ I_{cb}^* \\ I_{cc}^* \end{bmatrix} = \frac{1}{v_\alpha^2 + v_\beta^2} \begin{bmatrix} v_\alpha & -v_\beta \\ v_\beta & v_\alpha \end{bmatrix} \begin{bmatrix} p \sim - P_{loss} + P_{PV} \\ -q \end{bmatrix} \tag{7}$$

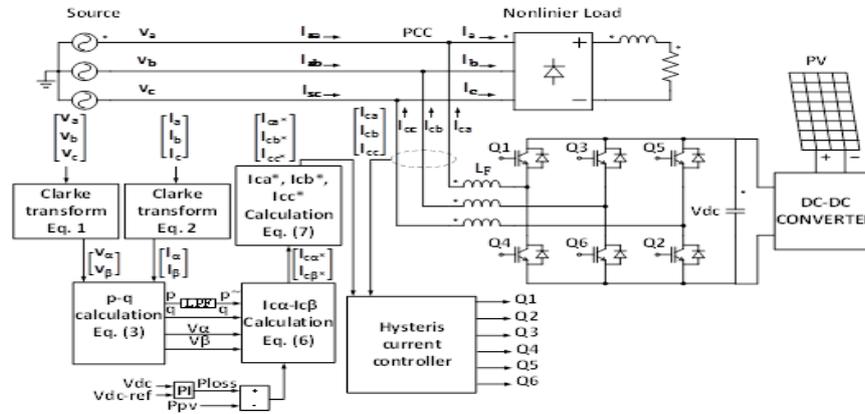


Figure 3. Block diagram of p-q Theory calculation

Reference current in Equation (7) is then transformed from the  $\alpha\beta$  coordinates into  $abc$  coordinate with Equation (8):

$$\begin{bmatrix} I_{ca}^* \\ I_{cb}^* \\ I_{cc}^* \end{bmatrix} = \sqrt{\frac{2}{3}} \begin{bmatrix} 1 & 0 \\ -1 & \sqrt{3} \\ 2 & 2 \\ -1 & -\sqrt{3} \\ 2 & 2 \end{bmatrix} \begin{bmatrix} I_{ca}^* \\ I_{cb}^* \end{bmatrix} \tag{8}$$

**2.3. Parameter**

Table 1 shows the parameters that used in the simulation of shunt active power filter in the active filter in photovoltaic grid-connected system.

Table 1. The Parameter Value of Shunt Active Power Filter Coupled Photovoltaic

Parameters	Value
V <sub>Source</sub>	3ϕ 380 volt
frequency	50 Hz
Load	6-pulsa rectifier 1700 watt, 10 var
V <sub>DC</sub>	850 volt
DC-link capacitor	20 uF
L <sub>F</sub> Inductor	55 mH
P <sub>PV</sub>	250 watt
PI constans	K <sub>p</sub> =10, K <sub>i</sub> =15
Converter component	L <sub>1</sub> =25 μH, L <sub>2</sub> =150 μH, C <sub>1</sub> =68,544 μF, C <sub>2</sub> =52,735 μF

**3. RESULT AND ANALYSIS**

SAPF+PV system configuration as shown in Figure 2 is simulated with MATLAB / Simulink to determine the performance of the system. Time sampling is 0.000006s. The scenario which was performed during the simulation includes, power flows from the source, PV and load. Simulations time line performed during 0.2s. For the firs 0.1s, the system is operated as pure SAPF then for the next second power from PV is injected.

**3.1. Active Power And Reactive Power Of Shunt Active Power Filter In Photovoltaic Grid-Connected System**

Shunt active power filter coupled photovotaic actively controlled in order to supply the active and reactive power to the load or to the grid. Simulations conducted under a constant load 1700 watts and 210

var. The system serves as a pure SAPF at  $t=0.02\text{s}$  until  $t=0.1\text{s}$ , during this period, all of the needs of active power served by the source. Then in the period  $t=0.1\text{s}$  to  $t=0.2\text{s}$ , photovoltaic power is injected so that the needs of active power is supplied by photovoltaic. As for the reactive power, all the needs of the load served by the shunt active power filter. Figure 4 and Figure 5 respectively show the relationship between the active and reactive power of source, load, and SAPF+PV. The simulation results show that the SAPF+PV systems are already able to control the power flow of active and reactive power.

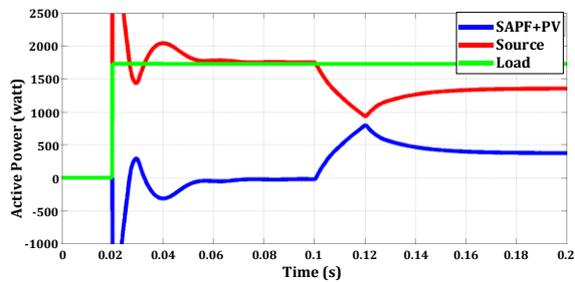


Figure 4. Active power curve of source, load and SAPF+PV

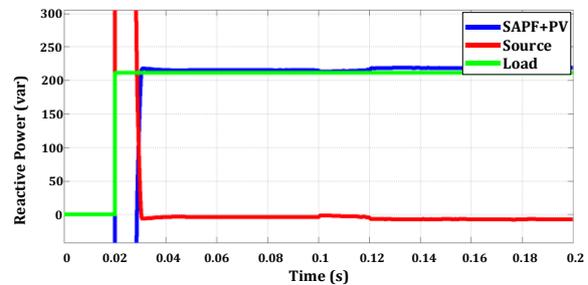


Figure 5. Reactive power curve of source, load and SAPF+PV

### 3.2. The Dc Side Voltage Of Of Shunt Active Power Filter In Photovoltaic Grid-Connected System

In accordance with the design, the DC side voltage is kept constant at a reference voltage of 850 volts. Figure 6 shows the DC side voltage can be kept constant according to the voltage reference despite the process of photovoltaic power injection at  $t=0.1\text{ s}$ . it indicates that the DC side voltage regulator is already working optimally.

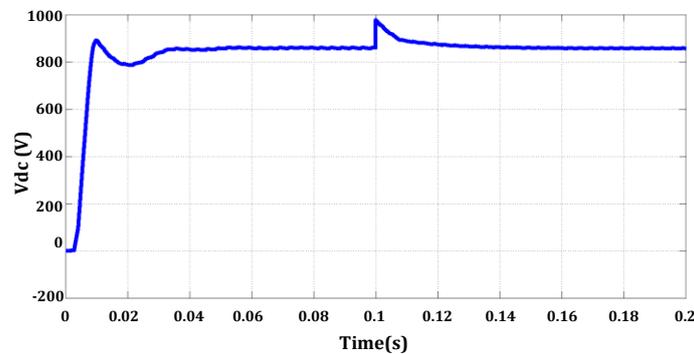


Figure 6. The DC side voltage of SAPF+PV

### 3.3. Shunt Active Power Filter Simulation In Photovoltaic Grid-Connected System

Figure 7 shows the simulation results of the shunt active power filter active in photovoltaic grid-connected system. The voltage that used in the calculation of the reference current is the voltage of each phase. compensation results show that the current resources has been a pure sinusoidal. In addition, the compensation current waveform is different at the time of photovoltaic injected active power into the grid.

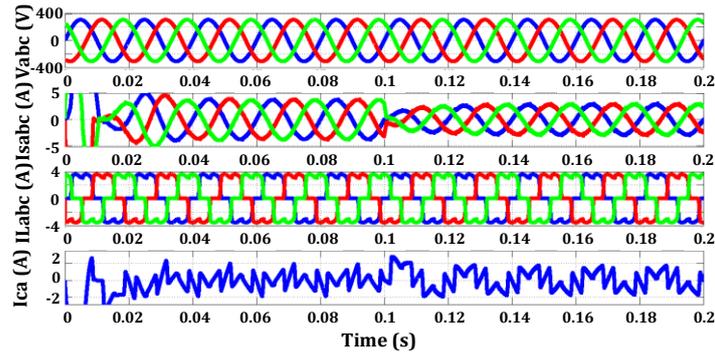


Figure 7. Simulation results of the shunt active power filter active in photovoltaic grid-connected system

In this study, analysis of harmonic component content is done by using Fast Fourier Transform (FFT) Analysis with the maximum frequency that used in the calculation of Total Harmonic Distorsion (THD) is 1000 Hz. The magnitude of the fundamental component and harmonic components expressed in percent units. The magnitude of the first order or the fundamental frequency would be 100%, which is the largest magnitude, whereas in the other order will be smaller than the first order. Figure 8-10 shows the harmonic spectrum in the time before and after compensated.

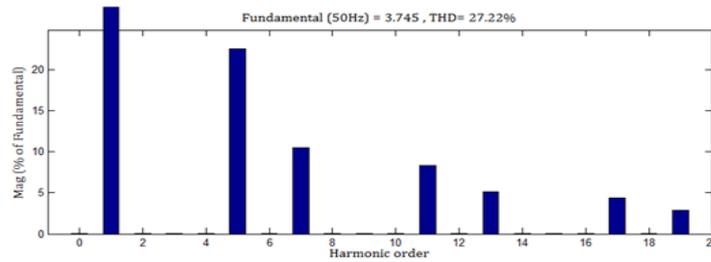


Figure 8. THD of current source before compensated

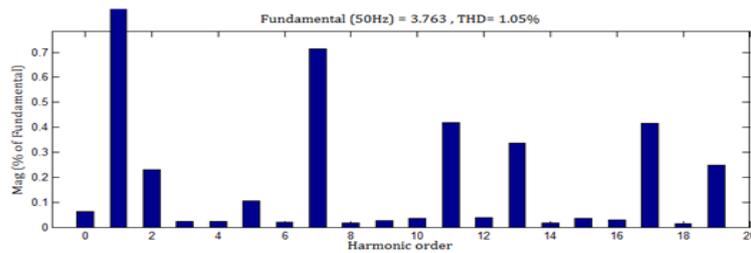


Figure 9. THD of current source before compensated in pure SAPF mode

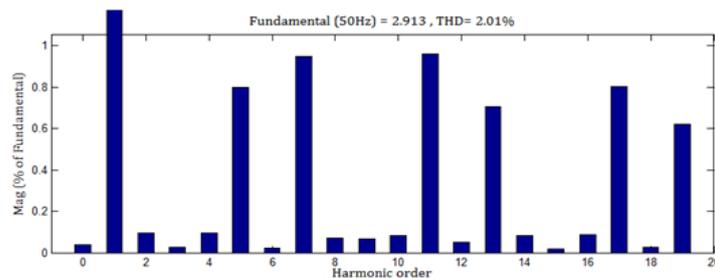


Figure 10. THD of current source before compensated in SAPF+PV mode

From the simulation results, the THD of current source before compensated is 27.22% as shown in Figure 8. Meanwhile, after the compensated, the THD of current source is 1.05% when the system is operating as a pure SAPF as shown in Figure 9. When SAPF coupled with PV, the THD of current source is 2.01% as shown in Figure 10.

#### 4. CONCLUSION

In this paper, the design of shunt active power filter based on p-q Theory in photovoltaic grid-connected system has been proposed. The p-q Theory is used to calculate the reference current. From the simulation results, can be obtained some key points as follows:

- a Vdc voltage can be kept constant corresponding reference voltage of 850 Volt.
- b Control of active and reactive power flow can work according to the p-q Theory.
- c SAPF+PV systems are designed to reduce the value of THD that generated by 6-pulse rectifier 1700 Watt from 27.22% to 1.05%. While, when the active power from photovoltaic is injected, the THD becomes 2.01%.

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